

Q (1)

- (a) Find all values of z such that $\cosh z = 1 + i$
- (b) Find an analytic function whose real part is $U(x, y) = x^3y - y^3x$.
- (c) Evaluate (i) $\oint_C \frac{\sin(\pi z^2)}{(z-1)^2(z-2)} dz$ where C is the circle $|z| = 3$
- (ii) $\oint_C \frac{\cosh(\frac{3}{z-1})}{(z-1)(z-3)} dz$ where C is the circle $|z| = 5$

Q (2)

- (a) Define the convex fuzzy set and determine whether the following fuzzy sets are convex or not $A = \int \frac{\mu_A(x)}{x}$, $\mu_A(x) = \begin{cases} 0 & x \leq 4 \\ \frac{1}{1+(x-4)^{-2}} & x > 4 \end{cases}$ then determine α -cut sets of the above set for $\alpha = 0.5$ and $\alpha = 0.9$.
- (b) A product with memberships represents, degree of high expensive $\mu_A(x)$, degree of medium expensive $\mu_B(x)$ and degree of cheap expensive $\mu_C(x)$. Use defuzzification methods to find suitable price if its cheap degree is 0.2, its medium degree is 0.5 and high degree 0.7 where

